



# The molecular basis of CO<sub>2</sub> interaction with polymers containing fluorinated groups: computational chemistry of model compounds and molecular simulation of poly[bis(2,2,2-trifluoroethoxy)phosphazene]

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Received 4 February 2003; received in revised form 24 March 2003; accepted 24 March 2003

## Abstract

Ab initio molecular orbital calculations of CO<sub>2</sub> and model compounds have been used to identify the nature of specific interactions between CO<sub>2</sub> and the fluorinated substituent groups of polymers such as poly(trifluoropropyl methyl siloxane) and poly[bis(2,2,2-trifluoroethoxy)phosphazene] (PTFEP) that exhibits high CO<sub>2</sub> permeability and permselectivity. Second-order Møller–Plesset (MP2) perturbation calculations (6-311++G\*\* basis set) were used to obtain energies, dipole and quadrupole moments, and polarizabilities of CO<sub>2</sub>, three alkanes (CH<sub>4</sub>, CH<sub>3</sub>CH<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>), and three fluoroalkanes (CF<sub>4</sub>, CH<sub>3</sub>CF<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>). Results of energy calculations of three CO<sub>2</sub>–alkane and three CO<sub>2</sub>–fluoroalkane dimers indicate that CO<sub>2</sub> forms a favorable quadrupole–dipole interaction with the fluoroalkyl groups. The maximum quadrupole–dipole interaction energy obtained was  $-11.5 \text{ kJ mol}^{-1}$  for CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>. This value is less than interaction energies typical for hydrogen bonding but greater than the London dispersion values reported for the interaction of CO<sub>2</sub> with the carbonyl group of poly(methyl methacrylate) (PMMA). Electrostatic potential distributions indicate a small redistribution of electron density to the fluorine atoms of the trifluoroalkanes and to the oxygen atoms of CO<sub>2</sub> in the CO<sub>2</sub>–CF<sub>3</sub>CH<sub>3</sub> and CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub> dimers.

Sorption and molecular association of CO<sub>2</sub> with PTFEP has been investigated by molecular simulation of an amorphous cell using the COMPASS molecular mechanics force field. CO<sub>2</sub> sorption isotherms obtained by Grand Canonical Monte Carlo (GCMC) simulation indicate an upward deviation from the linear relationship between  $\log S$  and the Lennard–Jones potential well depth parameter,  $\epsilon/k$ , in agreement with reported permeability data. Pair-correlation analysis obtained from molecular dynamics simulation show strong correlation of CO<sub>2</sub> with the trifluoromethyl group of PTFEP in agreement with the MP2 results showing an association of CO<sub>2</sub> with both CH<sub>3</sub>CF<sub>3</sub> and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>.

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**Keywords:** Carbon dioxide; Solubility; Molecular association

## 1. Introduction

It has been widely observed that many fluorinated compounds including simple fluorocarbons [1,2] and many fluorine-containing polymers such as vinylidene fluoride polymers [3] and perfluoropolymers including polytetrafluoroethylene [4] can be dissolved by supercritical CO<sub>2</sub> at high temperature and pressure. In addition, several studies have reported high solubility of CO<sub>2</sub> in some fluorine-containing polymers [5,6]. The basis for this

behavior has been the subject of some speculation and interest due to the attractive permselectivity of these polymers for CO<sub>2</sub> in mixtures with other gases such as methane. Examples of polymers reported to exhibit enhanced CO<sub>2</sub> permeability include poly(trifluoropropyl methyl siloxane) (PTFPMS) [6], some fluorine-containing polycarbonates [7] and polyimides [8,9], poly(vinylidene fluoride) (PVDF) [10,11], poly[*o*-(trifluoromethyl)phenylacetylene] (TFMPA) [12], fluorine-containing norbornene polymers [13], and poly[bis(2,2,2-trifluoroethoxy)phosphazene] (PTFEP) [14]. Structures of these polymers are shown in Table 1 to illustrate the location of accessible fluorine sites.

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Table 1  
Structures of fluorine-containing polymers

Polymer	Structure
Poly(trifluoropropyl methyl siloxane) (PTFPMS)	
Poly[ <i>o</i> -(trifluoromethyl)phenylacetylene] (PTFMPA)	
Tetramethylhexafluorobisphenol-A polycarbonate (TMHF-PC)	
Hexafluorobisphenol-A polycarbonate (HFPC)	
6FDA-4,4'-ODA <sup>a</sup> polyimide	
6FDA-DAF <sup>b</sup> polyimide	
6FDA-BAHF <sup>c</sup> polyimide	
Poly[5,5-difluoro-6,6-bis(trifluoromethyl)-norbornene] (PFMNB)	
Poly(vinylidene fluoride) (PVDF)	
Poly[bis(2,2,2-trifluoroethoxy)phosphazene] (PTFEP)	

<sup>a</sup> ODA: 4,4'-oxydianiline.

<sup>b</sup> DAF, diamino fluorene.

<sup>c</sup> 2,2-Bis(3,4-dicarboxyphenyl)hexafluoropropane dianhydride/2,2-bis(4-aminophenyl)hexafluoropropane.

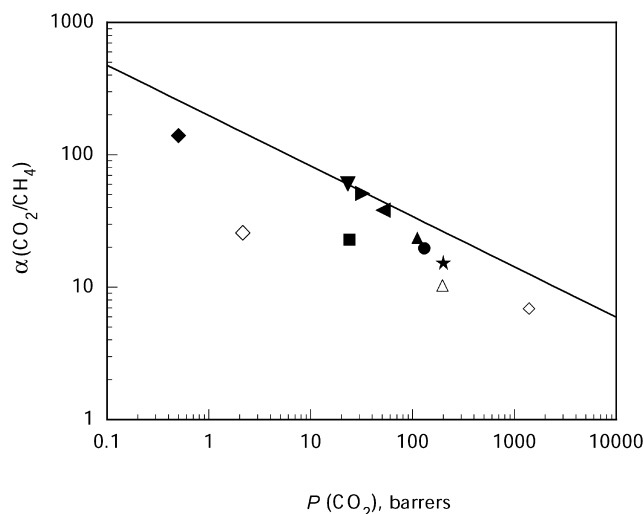


Fig. 1. Logarithmic plot of the ideal permselectivity of CO<sub>2</sub>/CH<sub>4</sub> versus CO<sub>2</sub> permeability. Line represents Robeson [15] boundary. Data points for PTFEP (△), PTFMPA (●), PTFPMS (◇), HFPC (■), TMHF-PC (▲), PVDF (◇), 6FDA-ODA (▼), 6FDA-DAF (►), 6FDA-BAHF (◄), PMMA (◆), and PFMNB (★). Closed symbols represent glassy polymers; open symbols represent rubbery polymers. See Table 1 for polymer structures.

The potential of a given polymer for a particular separation, such as CO<sub>2</sub> from a mixture with CH<sub>4</sub>, can be assessed from a plot of ideal permselectivity, the ratio of permeabilities of the two pure gases in the form

$$\alpha_{\text{CO}_2/\text{CH}_4} = \frac{P(\text{CO}_2)}{P(\text{CH}_4)} \quad (1)$$

versus permeability,  $P(\text{CO}_2)$ . Permselectivities of the fluorinated polymers cited previously are plotted against their CO<sub>2</sub> permeabilities in Fig. 1 and are compared to the Robeson [15] line delineating the upper boundary for CO<sub>2</sub>/

CH<sub>4</sub> given as

$$P_{\text{CO}_2}(\text{barrers}) = 1.0737 \times 10^6 (\alpha_{\text{CO}_2/\text{CH}_4})^{-2.6264} \quad (2)$$

This boundary marks the upper bound between CO<sub>2</sub>/CH<sub>4</sub> permselectivity and CO<sub>2</sub> permeability for approximately 300 glassy and rubbery polymers reported in the literature. With the exception of PVDF, which is highly crystalline and has low permeability, the fluorine-containing polymers have CO<sub>2</sub> permeabilities and permselectivities close to the boundary.

Stern and co-workers [5,6] has attributed the high solubility of CO<sub>2</sub> in simple fluoroalkane-substituted polymers such as PTFPMS, to a ‘specific interaction’ between CO<sub>2</sub> and the polar fluoroalkane groups of this polymer. In the case of poly(organophosphazenes), PTFEP exhibits the highest reported CO<sub>2</sub>/CH<sub>4</sub> permselectivity [16]. The high solubility of CO<sub>2</sub> in PTFEP has been attributed to interactions between CO<sub>2</sub> and the electron-withdrawing trifluoroethoxy group [14,17].

In the absence of specific interactions, the solubility of fixed gases can be correlated with various measures of the condensability [18] of the gas such as the critical temperature [5], boiling point [12], or the Lennard–Jones potential well-depth parameter,  $\epsilon/k$ , [10] in the form [19,20] of

$$\log S = \log S^0 + m(\epsilon/k) \quad (3)$$

As an approximation, the slope  $m$  is independent of the nature of the sorbing medium and is in the order of  $10^{-2} \text{ K}^{-1}$ . In a study by Hirose et al. [14], CO<sub>2</sub> solubility in PTFEP was found to be significantly higher than would be expected on the basis of this correlation. Similar observations were reported by Starannikova et al. [17] in a study of two PTFEP samples having different crystallinity. The elevated solubility of CO<sub>2</sub> in PTFEP is shown in Fig. 2 where  $\log S$  is plotted against  $\epsilon/k$ . Similar behavior is shown in Fig. 2 for PTFPMS and the fluorine-containing polynorbornene, PFMNB (see Table 1 for structures).

Since fluoroalkanes have high polarity and CO<sub>2</sub> is known to have a large quadrupole moment [21] as a result of its highly electronegative oxygen atoms, it is probable that the favorable interaction suggested by the solubility data may be due to a quadrupole–dipole interaction between CO<sub>2</sub> and the fluoroalkyl (or fluoroalkoxy) groups. In the first part of this study, dipole and quadrupole moments of CO<sub>2</sub>, three alkanes (CH<sub>4</sub>, CH<sub>3</sub>CH<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>), and three fluoroalkanes (CF<sub>4</sub>, CH<sub>3</sub>CF<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>) have been calculated using second-order Møller–Plesset perturbation (MP2) theory [22] and the 6-311++G\*\* basis set to incorporate electron correlation effects. In addition, total energies of CO<sub>2</sub> complexes with each of the alkanes and fluoroalkanes have been obtained from MP2/6-311++G\*\* calculations and the relative contributions of dipole and quadrupole interactions have been identified.

Molecular simulations have been used to investigate the

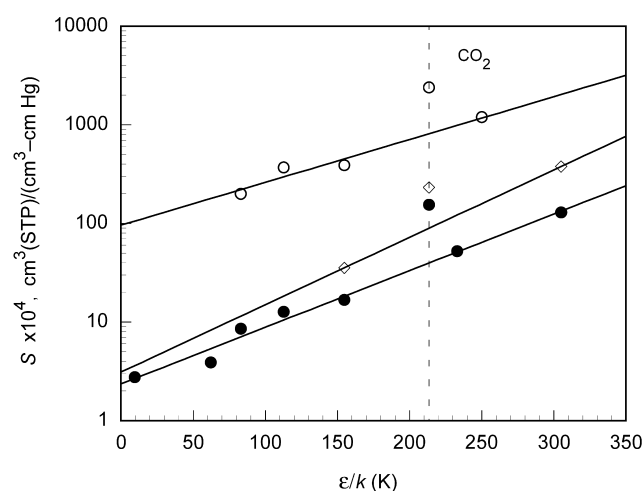


Fig. 2. Semilogarithmic plot of gas solubility versus the Lennard–Jones potential well-depth parameters,  $\epsilon/k$ . Solubility data: PTFEP (●), Hirose et al. [14]; PTFPMS (◇), Stern et al. [6]; PFMNB (○), Yampol'skii et al. [13]. Values of Lennard–Jones potential well-depth parameters were taken from Teplyakov and Meares [20]. Lines are drawn by least-square fit of experimental data with the exclusion of the CO<sub>2</sub> data point. Broken vertical line locates experimental solubility data for CO<sub>2</sub>.

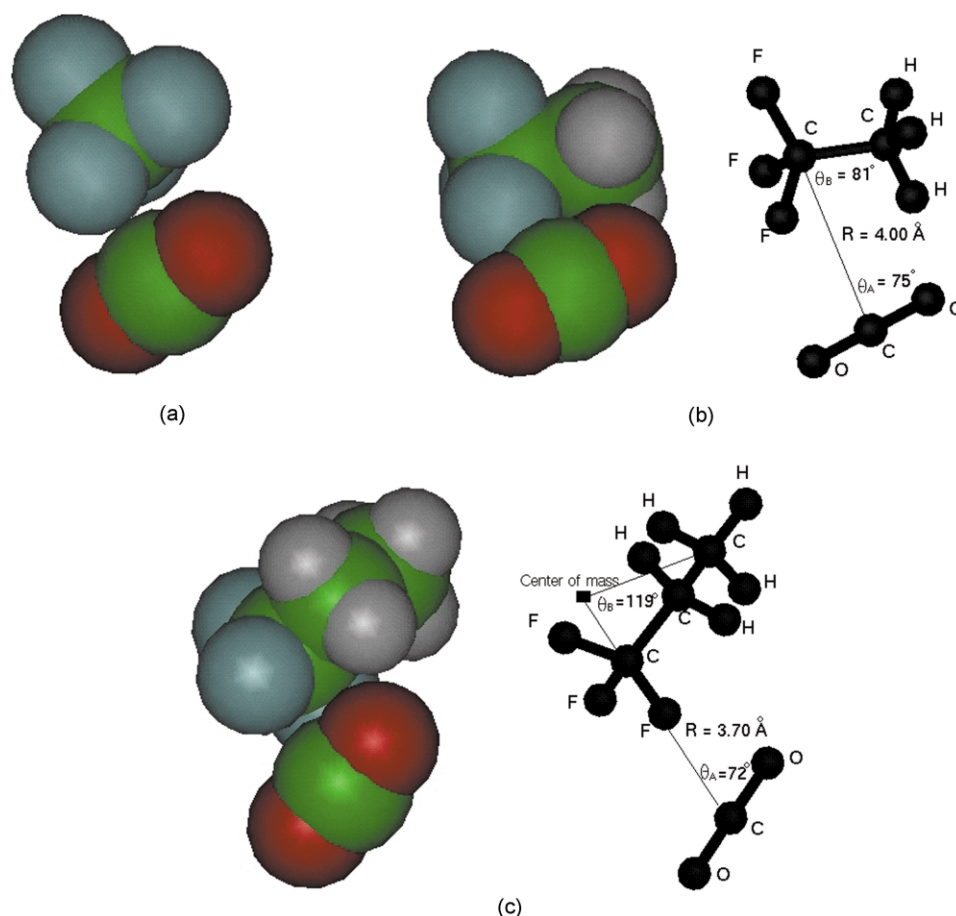


Fig. 3. (a) Space filling model showing energetically favorable interaction of CO<sub>2</sub> with tetrafluoromethane; (b) space filling and ball and stick representations of CO<sub>2</sub> interaction with trifluoroethane; (c) space filling and ball-and-stick representations of CO<sub>2</sub> interaction with trifluoropropane.

interaction of CO<sub>2</sub> with the fluoroethoxy group of PTFEP. Grand Canonical Monte Carlo (GCMC) simulation has been used to obtain solubility coefficients of He, N<sub>2</sub>, O<sub>2</sub>, CH<sub>4</sub>, CO<sub>2</sub>, and Xe; molecular dynamics has been used to investigate the association of CO<sub>2</sub> with the different atom positions and substituent groups of PTFEP by analysis of pair correlation functions. The force field used in these simulations is condensed-phase optimized molecular potentials for atomistic simulation studies (COMPASS) [23]. COMPASS is a class II ab initio force field that includes extensive use of cross terms and a 6–9 Lennard–Jones potential and a Coulombic expression for nonbonded terms. Details of individual force field terms in COMPASS have been given in earlier publications [23,24]. COMPASS has been parameterized and validated for polysilanes [25], alkanes and benzene compounds [23], and a variety of inorganic compounds and fixed gases [26]. Of particular importance to the present study, COMPASS has been extensively parameterized and validated for phosphazenes and polyorganophosphazenes [24] and has been successfully used to simulate the glass transition [27] and gas diffusion and solubility [28] of poly[bis(butoxyphosphazenes)].

## 2. Computational background

The elements of the quadrupole moment tensor were obtained as [29]

$$Q_{ij} = \int \sigma(\mathbf{r}) r_i r_j d\mathbf{r} \quad (4)$$

where  $\sigma(\mathbf{r})$  is the charge density distribution and  $r_i$  and  $r_j$  are the components of the distance vector from the molecular center. With CO<sub>2</sub> oriented along the  $x$ -axis and the carbon atom positioned at the origin, the off-diagonal elements become zero and the quadrupole moment is obtained as

$$\Theta = Q_{zz} - Q_{xx} \quad (5)$$

Polarizability was calculated as the average of the diagonal components of the polarizability tensor as

$$\alpha = \frac{1}{3}(\alpha_{xx} + \alpha_{yy} + \alpha_{zz}) \quad (6)$$

Dipole–quadrupole and quadrupole–quadrupole interaction energies were calculated from values of the dipole and quadrupole moments and the orientation angles,  $\theta$  and

$\phi$ , (see Fig. 3(b) and (c)) according to the equations [30]

$$U_{\mu\Theta} = \frac{\mu_A \Theta_B}{4\pi\epsilon_0 R^4} \frac{3}{2} [\cos \theta_A (3 \cos^2 \theta_B - 1) - 2 \sin \theta_A \times \sin \theta_B \cos \theta_B \cos \phi] \quad (7)$$

and

$$U_{\Theta\Theta} = \frac{\Theta_A \Theta_B}{4\pi\epsilon_0 R^5} \frac{3}{4} [1 - 5 \cos^2 \theta_A - 5 \cos^2 \theta_B - 15 \cos^2 \theta_A \cos^2 \theta_B + 2(4 \cos \theta_A \cos \theta_B - \sin \theta_A \sin \theta_B \cos \phi)^2] \quad (8)$$

where  $\epsilon_0$  is the dielectric permittivity of free space ( $8.854 \times 10^{-12} \text{ C}^2 \text{ J}^{-1} \text{ m}^{-1}$ ) and  $R$  is the distance between the centers of mass of the two interacting molecules as shown in Fig. 3(b) and (c).

The pair correlation coefficient (PCF),  $g_{\alpha\beta}(r)$ , provides a measure of the probability that, given the presence of an atom at the origin of an arbitrary reference frame, there will be an atom with its center located in a spherical shell of infinitesimal thickness at a distance  $r$  from the reference atom.

The solubility coefficients,  $S$ , were obtained from GCMC simulation of the sorption isotherms. In this procedure, a Metropolis [31] algorithm is used to accept or reject a configurational move (rotation and translation) and an insertion and deletion of a sorbate molecule. The configurational move is accepted if the energy change,  $\Delta U$ , is negative or if the Boltzmann factor,  $\exp(-\Delta U/kT)$  is greater than a random number generated between 0 and 1. Formally, the probability,  $P$ , of a move being accepted is expressed as

$$P = \min \left[ 1; \exp \left( \frac{-\Delta U}{kT} \right) \right]$$

where  $U$  is calculated from the sum of nonbonded (i.e. Coulombic and van der Waals interaction) energies. Similarly, the probabilities for addition and deletion of a sorbate molecule are given as

$$P_{\text{add}} = \min \left[ 1; \frac{1}{N+1} \frac{pV}{kT} \exp \left( \frac{-\Delta U}{kT} \right) \right]$$

and

$$P_{\text{del}} = \min \left[ 1; \frac{NkT}{pV} \exp \left( \frac{-\Delta U}{kT} \right) \right]$$

respectively, where  $N$  is the number of sorbate molecules. The solubility coefficient,  $S$ , is then obtained from the slope of the sorption isotherm as

$$S = \lim_{p \rightarrow 0} \frac{c}{p} \quad (9)$$

where  $c$  is the sorbed gas concentration, units of  $\text{cm}^3(\text{STP})/\text{cm}^3$  polymer, and  $p$  is pressure (cm Hg).

### 3. Computational procedures

**Ab initio studies.** Molecules of  $\text{CO}_2$ , the three alkanes ( $\text{CH}_4$ ,  $\text{CH}_3\text{CH}_3$ , and  $\text{CH}_3\text{CH}_2\text{CH}_3$ ), and three fluoroalkanes ( $\text{CF}_4$ ,  $\text{CH}_3\text{CF}_3$ , and  $\text{CH}_3\text{CH}_2\text{CF}_3$ ) were constructed using Spartan 5.1 (Wavefunction, Inc.). Their Z-matrix coordinates of each were imported to GAUSSIAN 94 running on a 12-processor (R-10010) SGI PowerChallengeXL server. Geometries were optimized (GAUSSIAN 94/Opt) using MP2/6-311++G\*\* and the polarizabilities, the dipole and quadrupole moments, and energies were obtained from single-point (MP2/6-311++G\*\*) calculations. The coordinates of the optimized structures were then exported to Spartan for calculation and display of the electrostatic potential distribution mapped on the electron density surface.

To form an equilibrated  $\text{CO}_2$  complex with ethane, propane, trifluoroethane, or trifluoropropane, both molecules were constructed and the energy of the system consisting of  $\text{CO}_2$  and the alkane or fluoroalkane was minimized by means of Insight II (Accelrys) using the COMPASS force field. The complex or dimer was further optimized using HF/3-21G\* in Spartan and then MP2/6-311++G\*\* in GAUSSIAN94. Electrostatic potentials of the dimers were then obtained by means of Spartan for comparison with the unpaired molecules.

**Molecular simulation.** Chains of PTFEP with 120 and 150 repeat units were prepared using an initial *cis-trans* conformation. The COMPASS force field described earlier and the charge group method for electrostatic interactions were used. For PTFEP, the neutral charge groups were  $\text{NP}(\text{OCH}_2)_2$  and  $\text{CF}_3$ . The polymer chain was then minimized for 1000 steps and used to construct a periodic amorphous cell using the explicit image convention. Based on a conventional RIS model, a stepwise chain construction scheme using the torsional potential obtained from COMPASS was used to generate the initial structure. Five different cells were prepared for both the 120 and 150-repeat unit cells. Additional details of the computational procedures are given elsewhere [32].

A 100-step minimization process was used to refine the resulting cells and eliminate any bad contacts (overlapping or close contacts of atoms). This was followed by an annealing procedure during which the periodic cell was heated from 300 to 600 K at intervals of 50 K and then cooled back to 298 K. At each step of the cycle, the cells were subject to 50-ps NPT dynamics. Next, 50-ps NVT dynamics was used to further relax the polymer structure with the cell density fixed at the average value obtained from previous 50 ps of NPT dynamics. This was followed by additional 150 ps of NPT dynamics. The first 50 ps of dynamics were discarded while the remaining 100 ps was saved as a history file.

The polymer cells with smallest energy and density variation during the final NPT dynamics run was selected from each set of five cells for GCMC simulation of



Table 2  
Results of MP2/6-311++G\*\* calculations

Compound	$\mu$ (D)	$\Theta$ (D Å)	MP2 energy (a.u.) <sup>a</sup>	$\alpha$ (Å <sup>3</sup> )
CO <sub>2</sub>	0	−4.62	−188.21	15.37
CH <sub>4</sub>	0	0	−40.38	14.04
CF <sub>4</sub>	0	0	−436.72	16.08
CH <sub>3</sub> CH <sub>3</sub>	0	−0.74	−79.57	25.89
CH <sub>3</sub> CF <sub>3</sub>	2.75	3.56	−376.84	26.59
CH <sub>3</sub> CH <sub>2</sub> CH <sub>3</sub>	0.086	0.54	−118.77	37.98
CH <sub>3</sub> CH <sub>2</sub> CF <sub>3</sub>	2.86	−0.76	−416.03	38.27

<sup>a</sup> 1 a.u. = 627.5095 kcal mol<sup>−1</sup> = 2629 kJ mol<sup>−1</sup>.

solubility at 298 K. The dimensions of the cell chosen from among the 120-r.u. cells was 30.9 Å; the 150-r.u. cell was slightly bigger at 32.9 Å. Based on studies of Wagner and co-workers [33,34], these box sizes are sufficiently large that simulation results for solubility should be reliable. Gas (He, N<sub>2</sub>, O<sub>2</sub>, CH<sub>4</sub>, CO<sub>2</sub>, or Xe) concentrations were determined at pressure increments of 0.5 atm over a range from 0 to 5 atm. A total of 200,000 steps were used for each sorption measurement (pressure and gas).

For PCF analysis of CO<sub>2</sub> interatomic interactions, four CO<sub>2</sub> molecules were inserted in an amorphous cell of PTFEP in such a manner that the distance between any two CO<sub>2</sub> molecules was more than half of the cell length. Next, 2 ns of NVT dynamics were run using the Anderson [35] temperature control algorithm, a 1.0 Å spline width, and a 12 Å cutoff for nonbonded interactions. Trajectory files were recorded at intervals of 1 ps. PCFs were calculated from 1 ns trajectories over 1.5 ns of NPT dynamics at 300 K. Van der Waals radii were obtained from the 6–9 Lennard–Jones expression used by COMPASS. For analysis of PCF distributions, trajectory frames were loaded into memory and different functional groups were assigned as subsets. PCF distributions for different CO<sub>2</sub>–functional group pairs were obtained by the Amorphous\_Cell/Analysis module of InsightII. The average PCF for CO<sub>2</sub> with different atoms of PTFEP was calculated as

$$g_i(r) = \frac{N_i(r)}{\rho_i N_{\text{CO}_2} N_S 4\pi r^2 dr} \quad (10)$$

where  $N_i(r)$  is the number of atoms of type  $i$  in a spherical shell between  $r$  and  $r + dr$ ,  $\rho_i$  is the bulk density of atoms of

type  $i$  in PTFEP,  $N_S$  is the total number of frames used for the analysis, and  $N_{\text{CO}_2}$  is the number of CO<sub>2</sub> molecules.

## 4. Results and discussion

*Ab initio studies.* As shown by values in Table 2, MP2/6-311++G\*\* calculations yield a value of −4.62 D Å for the quadrupole of CO<sub>2</sub>. This compares favorably with the established experimental value of −4.3 D Å [21]. Dehomelle et al. [36] reported a value of −4.13 D Å from MP2/VDJ calculations. Glaser et al. [29] have compared values using different basis sets at the RH, MP2, and QCISD(fc) levels of theory. At MP2/6-311 + G\*\*, their value for the quadrupole is −4.59 D Å which is very close to the value of −4.62 obtained in this study for MP2/6-311++G\*\*. In their study, a value of −4.28 D Å was obtained at the very highest computational level of QCISD/cc-pVTZ + . As shown by values given in Table 2, only CH<sub>3</sub>CF<sub>3</sub> and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub> have appreciable dipole moments; CH<sub>4</sub> and CF<sub>4</sub> have neither dipole nor quadrupole moments. As shown by values given in Table 2, there are no significant differences in polarizabilities between the fluorinated and nonfluorinated alkanes.

As shown in Fig. 3, dimer orientations indicate clear association between the carbon of CO<sub>2</sub> and the fluorine atoms of CF<sub>4</sub>, CH<sub>3</sub>CF<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>. Interaction energies were calculated as the difference between the total energy of the CO<sub>2</sub>–alkane or CO<sub>2</sub>–fluoroalkane dimer and the sum of the energies of CO<sub>2</sub> and the alkane or fluoroalkane (Table 2). As shown in Table 3, interaction energies between CO<sub>2</sub> and the fluoroalkanes are approximately twice the magnitude of the corresponding CO<sub>2</sub>–alkane interactions. The strongest interactions occur between CO<sub>2</sub> and CH<sub>3</sub>CF<sub>3</sub> and particularly between CO<sub>2</sub> and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub> for which there is a significant dipole–quadrupole interaction. Interaction energies for CO<sub>2</sub>–CF<sub>3</sub>CH<sub>3</sub> and CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub> are −8.92 and −11.5 kJ mol<sup>−1</sup>, respectively. In the case of CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>, approximately half of the total interaction energy is due to dipole–quadrupole interaction. It is noted that the interaction energy between CO<sub>2</sub> and propane is smaller (−6.88 kJ mol<sup>−1</sup>) but not

Table 3  
MP2/6-311++G\*\* energies of CO<sub>2</sub> dimers

Dimer	$R$ (Å)	Total energy (a.u.)	Interaction energy	$U_{\mu\Theta}$	$U_{\Theta\Theta}$	Other <sup>a</sup>
CO <sub>2</sub> –CH <sub>4</sub>	3.52	−228.59	−3.14	0	0	−3.14
CO <sub>2</sub> –CF <sub>4</sub>	3.84	−624.93	−6.04	0	0	−6.04
CO <sub>2</sub> –CH <sub>3</sub> CH <sub>3</sub>	3.54	−267.78	−5.17	0	0	−5.17
CO <sub>2</sub> –CF <sub>3</sub> CH <sub>3</sub>	3.96	−565.05	−8.92	−2.12	0.617	−7.42
CO <sub>2</sub> –CF <sub>3</sub> CH <sub>2</sub> CH <sub>3</sub>	3.57	−306.98	−6.88	0	0	−6.88
CO <sub>2</sub> –CF <sub>3</sub> CH <sub>2</sub> CH <sub>3</sub>	3.73	−604.25	−11.5	−6.01	−1.34	−4.11

Unless otherwise indicated, units are kJ mol<sup>−1</sup>.

<sup>a</sup> Dispersion, induction, and electrostatic (other than dipole and quadrupole terms).

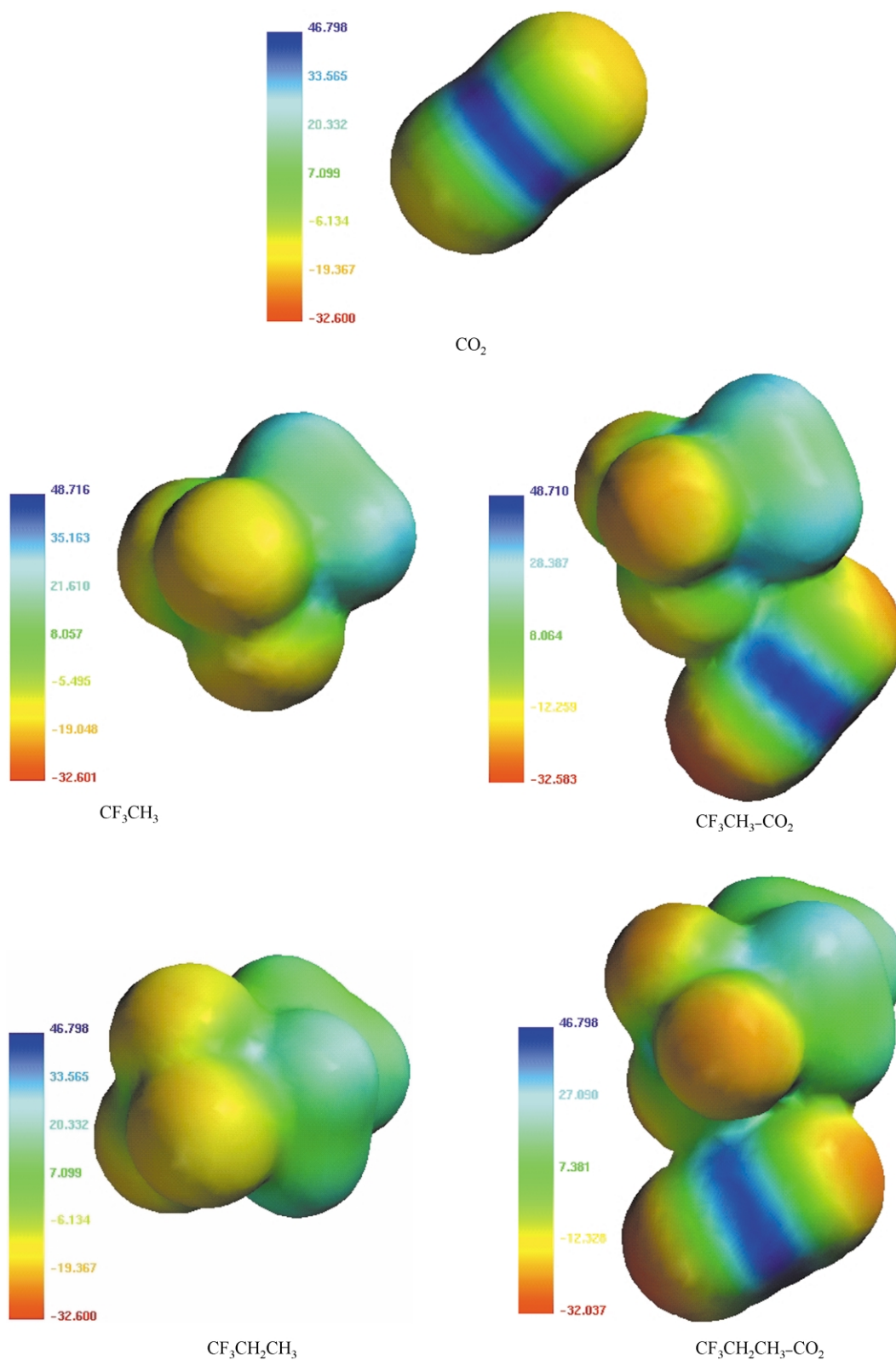


Fig. 4. Mapping of electrostatic distribution on the electron density surfaces of CO<sub>2</sub>, CF<sub>3</sub>CH<sub>3</sub>, CF<sub>3</sub>CH<sub>3</sub>-CO<sub>2</sub>, CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub>-CO<sub>2</sub>. Red regions indicate areas of high electronegativity; blue regions indicate areas of high positive charge.

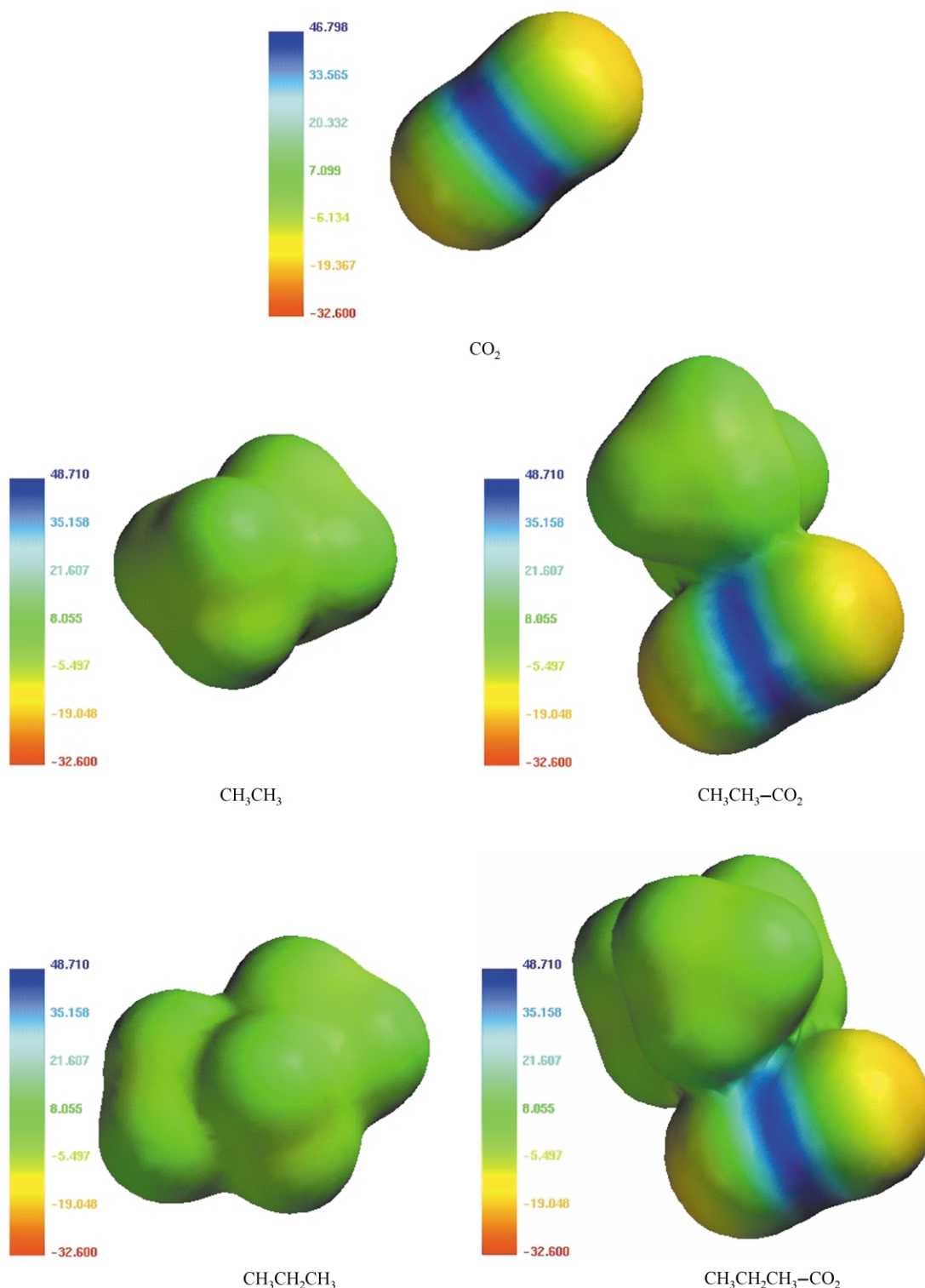


Fig. 5. Mapping of electrostatic distribution on the electron density surfaces of  $\text{CO}_2$ ,  $\text{CH}_3\text{CH}_3$ ,  $\text{CH}_3\text{CH}_3\text{-CO}_2$ ,  $\text{CH}_3\text{CH}_2\text{CH}_3$ , and  $\text{CH}_3\text{CH}_2\text{CH}_3\text{-CO}_2$ .

negligible in the absence of a dipole–quadrupole interaction and may be attributed to dispersion and other interactions [36].

It should be noted that the magnitudes of the interaction energies for  $\text{CO}_2\text{-CF}_3\text{CH}_3$  and  $\text{CO}_2\text{-CF}_3\text{-CH}_2\text{CH}_3$  lie below the range typically reported for

hydrogen bonding (i.e.  $12\text{--}30\text{ kJ mol}^{-1}$ ) [30] but are larger than observed for  $\text{CO}_2$  and poly(methyl methacrylate) (PMMA). PMMA also exhibits high  $\text{CO}_2$  permselectivity as shown in Fig. 1 and has been reported to exhibit elevated  $\text{CO}_2$  solubility [11]. From FTIR measurements, Kazarian et al. [37] obtained a



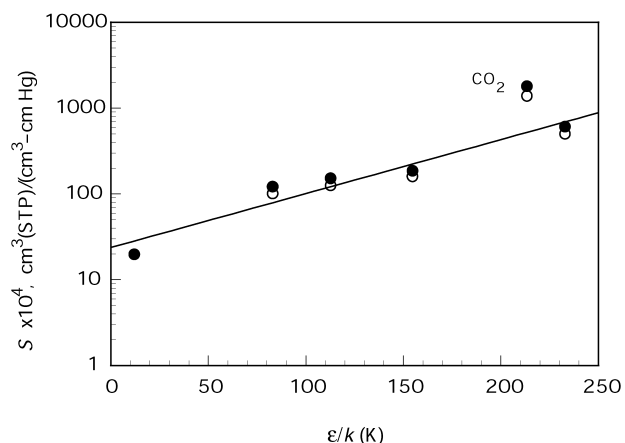


Fig. 6. Semilogarithmic plot of gas solubility obtained at 298 K from GCMC simulation of a 120-repeat unit (○) and 150-repeat unit cell (●) versus the Lennard-Jones potential well-depth parameters,  $\epsilon/k$ , of He, N<sub>2</sub>, O<sub>2</sub>, CH<sub>4</sub>, CO<sub>2</sub>, and Xe. Lennard-Jones potential well-depth parameters were taken from Teplyakov and Meares [20]. The line represents the least-square fit ( $R^2 = 0.9320$ ) of simulation data for the 150 repeat unit cell with the exclusion of the CO<sub>2</sub> data point.

value of  $4.2 \text{ kJ mol}^{-1}$  that they attributed to a Lewis acid–base interaction of CO<sub>2</sub> with the carbonyl group of PMMA.

Electrostatic potentials are mapped onto the electron density surfaces of CO<sub>2</sub>, CH<sub>3</sub>CF<sub>3</sub>, and CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub> in Fig. 4. Comparison with the electrostatic potentials for the CO<sub>2</sub>–CF<sub>3</sub>CH<sub>3</sub> and CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub> dimers indicate the appearance of a reddish orange coloration at the tops of the fluorine atoms of the fluoroalkanes and the oxygens atoms of CO<sub>2</sub>. The prominence of red coloration is somewhat more intense for the oxygen closest to the fluorine atoms. These visual indications of electron redistribution are evident in small changes in the ESP charges as well. For example, ESP charges on fluorine decreases from  $-0.26$  for CH<sub>3</sub>CF<sub>3</sub> to  $-0.29$  for CO<sub>2</sub>–CF<sub>3</sub>CH<sub>3</sub> and from  $-0.28$  for CH<sub>3</sub>CH<sub>2</sub>CF<sub>3</sub> to  $-0.29$  for CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>. In the case of CO<sub>2</sub>, the

ESP charge of the oxygen atom closest to fluorine decreases from  $-0.439$  to  $-0.465$  for CO<sub>2</sub>–CH<sub>3</sub>CF<sub>3</sub> and from  $-0.439$  to  $-0.468$  for CO<sub>2</sub>–CF<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>. As shown in Fig. 5, this small change in electron distribution for the oxygen sites of CO<sub>2</sub> does not occur in the case of the alkane dimers. For CO<sub>2</sub>–CH<sub>3</sub>CH<sub>3</sub>, the ESP charges for both oxygen atoms of CO<sub>2</sub> are equal and only change from  $-0.439$  to  $-0.445$  and from  $-0.439$  to  $-0.445$  for CO<sub>2</sub>–CH<sub>3</sub>CH<sub>2</sub>CH<sub>3</sub>.

**Molecular simulations.** As shown in Fig. 6, gas solubility coefficients obtained from GCMC simulations at 298 K follow closely the correlation given by Eq. (3) with the exception of the CO<sub>2</sub> solubility which lies above the correlation relationship as previously shown from permeability data for PTFEP and two other fluorine-containing polymers in Fig. 2. The line representing a least-squares fit ( $R^2 = 0.9320$ ) of the five data points (excluding CO<sub>2</sub>) obtained for the 150-r.u. periodic cell (32.9 Å) has a slope of  $3.3 \times 10^{-2} \text{ K}^{-1}$  which is consistent with data for other polymers. As shown in Fig. 6, sorption data for a slightly smaller (30.9 Å) cell obtained by building an amorphous cell from a 120-r.u. cell indicate good reproducibility of the results. There is also good qualitative agreement with the experimental data for a semicrystalline (60%) sample [14] as was shown in Fig. 2; however, solubility values for the semicrystalline samples are smaller than obtained for the amorphous state of the simulation as would be expected. As will be reported in a subsequent report [38], GCMC simulation of the crystalline forms of PTFEP confirm that gas solubility is negligible in comparison with the amorphous state.

In Fig. 7, averaged pair correlation functions are plotted against separation distance for the phosphorus and nitrogen atoms along the backbone of PTFEP and for the CH<sub>2</sub> and CF<sub>3</sub> groups and the oxygen atoms in the side chains. In the case of polydimethylphosphazene, Gallazzi et al. [39] have suggested that the lone pair electrons of the nitrogen atom along the polymer backbone could participate in donor–acceptor interaction with carbon dioxide; however, the results for N in the case of PTFEP do not indicate any preferential interaction of CO<sub>2</sub> with nitrogen. As shown in Fig. 7, association is the strongest for CO<sub>2</sub> with CF<sub>3</sub> and second strongest for CO<sub>2</sub> with the CH<sub>2</sub> group that is attached directly to CF<sub>3</sub>. These MD results are consistent with the previously discussed ab initio calculations that indicate a specific (i.e. dipole–quadrupole) interaction between CO<sub>2</sub> and the CF<sub>3</sub> group of trifluoroethane or trifluoropropane. The separation between CO<sub>2</sub> and the CF<sub>3</sub> group of PTFEP at the maximum of the PCF is approximately  $4.3 \text{ Å}$  which is only slightly larger than the ab initio results for CO<sub>2</sub> and the fluoroalkanes in Fig. 3(b) and (c). The sharpness of the peak for CO<sub>2</sub>–CF<sub>3</sub> appearing in the PCF plot of Fig. 7 is a strong evidence for preferential association of CO<sub>2</sub> with the trifluoroethoxy group of PTFEP.

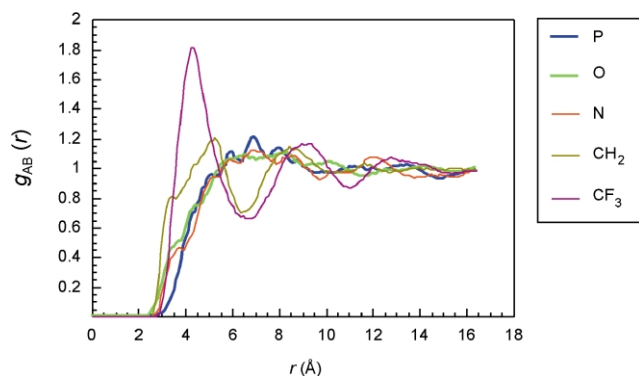


Fig. 7. Plot of the pair correlation function,  $g_{AB}(r)$ , versus the separation distance,  $r$  (Å), between CO<sub>2</sub> and the phosphorus and nitrogen atoms along the chain backbone and between CO<sub>2</sub> and the oxygen atoms, methylene groups, and trifluoromethyl groups of the trifluoroethoxy side chains of PTFEP.

## 5. Conclusions

Results of *ab initio* (MP2/6-311++G\*\* ) calculations indicate favorable interaction between CO<sub>2</sub> and the polar fluoromethyl group of trifluoroethane and trifluoropropane. Analysis of the data suggests that quadrupole–dipole interaction is an important contribution to the total energy of interaction. These conclusions of specific association are consistent with results of GCMC simulation of solubility and molecular dynamics simulation of pair correlations of CO<sub>2</sub> with the trifluoromethyl group of PTFEP. Preferential association of CO<sub>2</sub> may occur on a similar basis of quadrupole–dipole interaction with the accessible fluorine sites of other polymers such as PTFPMS that also exhibit high CO<sub>2</sub> solubility. It is clear from the *ab initio* and molecular dynamics simulations reported in the present study that close physical association (less than 4.3 Å between centers of mass) is necessary. For some polymers with bulky groups, perhaps including 6F polyimides and related polymers (see Table 1), such close contacts may not be possible and other contributions such as increased free volume due to steric repulsions may lead to high solubility and permselectivity.

## Acknowledgements

Major support from the Ohio Board of Regents (Investment Fund) for computer facilities and software used in these studies is greatly appreciated. This material is based partially upon work supported by the National Science Foundation under Grant no. 9810320.

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